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Molecular dynamics/hydrodynamics hybrid description of liquids and biomolecular solutions

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The talk's plan:

- I. Hybrid MD/HD framework
- II. Mercedes-Benz water
- III. Long-range order in water dynamics and its reduction by a peptide solute

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Hybrid MD/HD: motivation

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Motivation: true *multiscaling*





Hybrid MD/HD: hydrodynamics

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Continuous representation (hydrodynamics)

- All started with macroscopic thermodynamical quantities: the properties of the system **as a whole**, the largest possible scale.
- Describing the system at smaller scales: the properties become **fields** changing in **time**:

 $\rho(\mathbf{x},t), \mathbf{u}(\mathbf{x},t), T(\mathbf{x},t).$

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- ${\bf x}$ is the Euclidean 3D space.
- The equations of motion are the HD equations.
- The solution is the values of the fields at each location in space at every instant of time: $\rho(\mathbf{x}, t), \mathbf{u}(\mathbf{x}, t), T(\mathbf{x}, t)$.



Hybrid MD/HD: atomistic

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Atomistic representation

- The variables are the positions and momenta of the point masses, the atoms:

$$\{\mathbf{q}_1,\ldots,\mathbf{q}_N,\mathbf{p}_1,\ldots,\mathbf{p}_N\}$$

- The space is the $6N\mbox{-dimensional}$ phase space.
- The atoms interact through empirically (in MD) defined Hamiltonian $H({\bf q},{\bf p})$
- The equations of motion describing $\mathbf{q}(t),\mathbf{p}(t)$ are the Hamilton equations

$$\frac{\mathrm{d}q_i(t)}{\mathrm{d}t} = \frac{\partial H(\mathbf{q},\mathbf{p})}{\partial p_i}, \frac{\mathrm{d}p_i(t)}{\mathrm{d}t} = -\frac{\partial H(\mathbf{q},\mathbf{p})}{\partial q_i}$$

- The solution is the molecular trajectory: the values of the coordinates and momenta at every moment of time:

$$\mathbf{q}(t), \mathbf{p}(t).$$

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Connecting the representations

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- The end domains HD and MD are described by purely hydrodynamic and purely Newtonian equations of motion respectively.
- In the hybrid domain the fluid consists of two "phases":
 - HD phase is a continuum water with volume fraction $s = \frac{V_1}{V}$,
 - MD phase is a phase that incorporates atoms, its volume fraction is (1 s).
- The parameter s = s(x) is the function of space coordinates (and, generally, time), such that s = 1 in the HD domain, s = 0 in the MD domain.



Mass conservation

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For HD phase:

$$\frac{\partial}{\partial t}\left(s\rho\right) + \frac{\partial}{\partial x_{i}}\left(u_{i}s\rho\right) = J,$$

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For MD phase:

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$$\frac{\partial}{\partial t} \left((1-s) \sum_{p=1,N(t)} \rho_p \right) + \frac{\partial}{\partial x_i} \left((1-s) \sum_{p=1,N(t)} \rho_p u_{ip} \right) = -J,$$

where $\rho_p = m_p/V$ is the density of MD particles and J is the birth/death rate due to the coupling between the phases.

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Modified MD equations

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MD velocities are constrained to HD phase in the $s \rightarrow 1$ limit:

$$\frac{dx_{ip}}{dt} = u_{ip} + s(u_i - u_{ip}) + s(1 - s)\alpha \frac{\partial}{\partial x_i} \left(\tilde{\rho} - \sum_{p=1,N(t)} \rho_p \right) / \rho_p / N(t),$$

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where $\tilde{\rho} = s\rho + (1-s)\sum_{p=1,N(t)}\rho_p$.



The source J

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From the modified MD the source J can be found:

$$J = s \frac{\partial}{\partial t} \sum_{p=1,N(t)} \rho_p + \frac{\partial}{\partial x_i} \left(su_i \sum_{p=1,N(t)} \rho_p \right) + \frac{\partial}{\partial x_i} \left(s(1-s)\alpha \frac{\partial}{\partial x_i} \left(\tilde{\rho} - \sum_{p=1,N(t)} \rho_p \right) \right),$$

where
$$\tilde{\rho} = s\rho + (1-s)\sum_{p=1,N(t)}\rho_p$$

 $\tilde{\rho}$ is diffused towards $\sum_{p=1,N(t)} \rho_p$:

$$\frac{D}{Dt}\left(\tilde{\rho} - \sum_{p=1,N(t)} \rho_p\right) = \frac{\partial}{\partial x_i} \left(s(1-s)\alpha \frac{\partial}{\partial x_i} \left(\tilde{\rho} - \sum_{p=1,N(t)} \rho_p\right)\right).$$



Conservation of momentum

For HD phase:

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 $\frac{\partial}{\partial t}\left(su_{i}\rho\right) + \frac{\partial}{\partial x_{i}}\left(u_{j}u_{i}s\rho\right) = sF_{i} + J_{2},$

where J_2 is the HD-MD interaction force and F_i is the hydrodynamic force, calculated from Landau-Lifshitz fluctuating hydrodynamics model:

$$F_{i} = -\frac{\partial T_{ij}^{FH}}{\partial x_{i}}$$

$$T_{ij}^{FH} = T_{ij} + \tilde{T}_{ij}$$

$$T_{ij} = \left(p - \xi \frac{\partial}{\partial x_{\alpha}} u_{\alpha}\right) \delta_{ij} - \nu \left(\frac{\partial}{\partial x_{i}} u_{j} + \frac{\partial}{\partial x_{j}} u_{i} - 2D^{-1} \frac{\partial}{\partial x_{\alpha}} u_{\alpha} \delta_{ij}\right)$$

where D is the problem dimension, p is pressure, ξ , ν are the (macro) viscosity coefficients, \tilde{T}_{ij} is a random Gaussian matrix with zero mean and correlations depending on the viscosities and k_BT .



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For MD phase:

$$\frac{\partial}{\partial t} \left((1-s) \sum_{p=1,N(t)} u_{i,p} \rho_p \right) + \frac{\partial}{\partial x_j} \left((1-s) \sum_{p=1,N(t)} \rho_p u_{i,p} u_{j,p} \right)$$
$$= (1-s) \sum_{p=1,N(t)} F_{i,p} - J_2$$

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Modified MD equation for the force

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Similarly to the modified equation for MD velocities:

$$\begin{split} \frac{du_{jp}}{dt} &= (1-s)F_{jp}/\rho_p + sF_j/\rho_p/N(t) \\ &+ \frac{\partial}{\partial x_i} \left(s(1-s)\alpha \sum_{p=1,N(t)} u_{jp}/N(t) \frac{\partial}{\partial x_i} \left(\tilde{\rho} - \sum_{p=1,N(t)} \rho_p \right) \right) \frac{1}{\rho_p N} \\ &- \frac{\partial}{\partial x_i} \left(s(1-s)\beta \frac{\partial}{\partial x_i} \left(\tilde{u}_j \tilde{\rho} - \sum_{p=1,N(t)} u_{jp} \rho_p \right) \right) / \rho_p/N(t), \end{split}$$

where
$$\tilde{\rho} = s\rho + (1-s)\sum_{p=1,N(t)}\rho_p$$
,
 $\tilde{u}_j = \left[s\rho u_j + (1-s)\sum_{p=1,N(t)}\rho_p u_{jp}\right]/\tilde{\rho}$.

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$$J_{2} = s \frac{\partial}{\partial t} \sum_{p=1,N(t)} \rho_{p} u_{jp} + \frac{\partial}{\partial x_{i}} \left(su_{i} \sum_{p=1,N(t)} \rho_{p} u_{jp} \right) - sF_{j} + \frac{\partial}{\partial x_{i}} \left(s(1-s)\beta \frac{\partial}{\partial x_{i}} \left(\tilde{u}_{j} \tilde{\rho} - \sum_{p=1,N(t)} u_{jp} \rho_{p} \right) \right),$$

where
$$\tilde{\rho} = s\rho + (1-s)\sum_{p=1,N(t)} \rho_p,$$

 $\tilde{u}_j = \left[s\rho u_j + (1-s)\sum_{p=1,N(t)} \rho_p u_{jp}\right]/\tilde{\rho}.$
 $\tilde{u}_j\tilde{\rho}$ is diffused towards $\sum_{p=1,N(t)} u_{jp}\rho_p$:

$$\frac{D}{Dt} \left(\tilde{u}_j \tilde{\rho} - \sum_{p=1,N(t)} u_{jp} \rho_p \right) = \frac{\partial}{\partial x_i} \left(s(1-s) \beta \frac{\partial}{\partial x_i} \left(\tilde{u}_j \tilde{\rho} - \sum_{\substack{p=1,N(t)\\ + \Box > i < \overline{\Box} > i < \overline{\Box} > i < \overline{\Xi} > i < \overline{\Xi} > i < \overline{\Xi} < \overline{\Box} < \overline{\Box} < \overline{\Box} > i < \overline{\Xi} > i < \overline{\Xi} > \overline{\Box} < \overline{\Box} > \overline{\Box} < \overline{\Box} > \overline{\Box} < \overline{\Box} > \overline{\Box} > \overline{\Box} < \overline{\Box} > \overline{\Box}$$



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Results for 2D Lennard-Jones liquid:



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- Atomistic and continuum representations of liquid can be connected seamlessly and consistently in space and time.
- The domains of each representations can be defined arbitrarily in space and time.
- The conceptual novelty: studying the properties of different representations at the same space and time scale; the flows *between* the representations.
- The advantage in applications: very substantial saving on computation at the HD domain without loosing the atomistic details of the core.

- Outlook: multiple scales, MD \rightarrow HD.



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$$\Phi = \Phi_{LJ} + \Phi_{HB},$$

where Φ_{LJ} is the Lennard-Jonnes potential, Φ_{HB} is the explicit hydrogen bonding term:

$$\Phi_{HB} = \epsilon_{HB} \cdot G(r_{ij} - r_{HB}) \sum_{ij}^{N} G(\vec{i}_k \cdot \vec{u}_{ij} - 1) G(\vec{j}_l \cdot \vec{u}_{ij} + 1),$$

G is the Gaussian function $G(x) = e^{\frac{-x^2}{2\sigma^2}}$.

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MB water snapshot



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The thermodynamic properties are expressed through K, $\frac{\partial \Phi}{\partial A}$ only: temperature: $T = \frac{2}{3N} \langle K \rangle$, pressure: $P = \rho \ k_B T - \langle \frac{\partial \Phi}{\partial A} \rangle$, isochoric heat capacity

$$\frac{C_V}{Nk_B} = \left(\frac{2}{3} \left\langle K \right\rangle \left\langle K^{-1} \right\rangle + N(1 - \left\langle K \right\rangle \left\langle K^{-1} \right\rangle)\right)^{-1}$$

$$K = \sum_{i=1}^{N} \frac{m\vec{v}_{i}^{2}}{2} + \frac{I\omega_{i}^{2}}{2},$$

where I is the moment of inertia, \vec{v}_i and ω_i are the translational and angle velocities.

$$\frac{d\Phi}{dA} = \frac{1}{2A} \sum_{i=1}^{N-1} \sum_{j=i+1}^{N} dx \frac{d\Phi_{ij}}{dx} + dy \frac{d\Phi_{ij}}{dy}.$$

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Figure : Isothermal compressibility β^* , pressure P^* , isochoric heat capacity C_V^* , isothermal expansion coefficient α^* .

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$$g_r^{(2)}(r) = \frac{2V}{N^2} \left\langle \sum_{i < j} \delta(r - |\vec{u}_{ij}|) \right\rangle,$$
$$g_{\phi}^{(2)}(r) = \frac{1}{Z_{ij}} \left\langle \sum_{i < j} z_{ij} \delta(r - |\vec{u}_{ij}|) \right\rangle,$$

$$z_{ij} = \sum_{k=1}^{3} \sum_{l=1}^{3} G(\vec{i}_k \cdot \vec{u}_{ij} - 1) G(\vec{j}_l \cdot \vec{u}_{ij} + 1),$$

$$Z_{ij} = \int_0^\infty \left\langle \sum_{i < j} z_{ij} \delta(r - |\vec{u}_{ij}|) \right\rangle dr,$$

where N is the number of molecules in the corresponding solvation shell, Z_{ij} is the normalization factor.





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Figure : Radial distribution function. The reference molecule is shown in green. The 'interstitial' water is red.

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Figure : Orientation contribution as a function of distance.

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The velocity autocorrelation function:

$$f_v(\tau) = \left\langle \vec{v}(t) \cdot \vec{v}(t+\tau) \right\rangle,\,$$

where $\vec{v}(t)$ and $\vec{v}(t+\tau)$ are translational velocities at time moments t and $t+\tau$.

The rotation velocity autocorrelation function:

$$f_{\omega}(\tau) = \left\langle \omega(t) \cdot \omega(t+\tau) \right\rangle,\,$$

where $\omega(t) = \frac{\partial \phi}{\partial t}$ is rotational velocity.



MB water dynamics



Figure : Velocity autocorrelation functions for MB and SPC models.

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- Two dimensional water qualitatively and sometimes quantitatively represents the properties of real water.
- Molecular dynamics of the model works well and reproduces the results of Monte Carlo.
- The usefulness of the model: N^2 dependence on system size, easy visualisation.

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Long-range order in water dynamics and its reduction by a peptide solute

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Small peptide in explicit water



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Symbolisation of MD simulated water





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L-long words of symbols:

$$s^L \equiv \{\mathbf{v}_{t-L+1} \dots \mathbf{v}_{t-2} \mathbf{v}_{t-1} \mathbf{v}_t\}$$

The Shannon entropy of words:

$$H(L) \equiv -\sum_{s^L} P(s^L) \log_2 P(s^L)$$

The entropy rate:

$$h_{\mu} \equiv \lim_{L \to \infty} \frac{H(L)}{L}$$

The excess entropy:

$$\mathbf{E} \equiv \sum_{L=1}^{\infty} [h_{\mu}(L) - h_{\mu}]$$

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"The excess entropy tells us how much information must be gained before it is possible to infer the actual per-symbol randomness h_{μ} . It is large if the system possesses many regularities or correlations that manifest themselves only at large scales." [D. Feldman *et al*, *Chaos*, **18**, 043106 (2008)]

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Excess entropy of water near peptide





Excess entropy: conclusion

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The background The model Mass conservation Momentum conservation	- Very long range order in water is present, which is significantly perturbed by the peptide.
Results	- The width of the hydration layer, the shell of water molecules affecting the peptide's dynamics, should be extended to
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